



## Performance assessment of a power/refrigeration cogeneration system driven by the waste heat of a solid oxide fuel cell

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### Abstract

A combination of a solid oxide fuel cell with two CCP subsystems to generate power and refrigeration is investigated in the present paper. The proposed system consists of two combined ORC-VCR systems whose input energy is supplied by the waste heat of a SOFC. Energy and exergy analysis was carried out for the system components. The results indicate that by recovering the waste heat of the SOFC, the energy and exergy efficiencies are improved by 45.82% and 6.14% compared to the stand-alone SOFC system. In addition, the proposed system can generate 382.4kW power and 176.28kW refrigeration, respectively. Moreover, the exergy analysis demonstrates that the air heat exchanger, afterburner, SOFC stack, and evaporator have a considerable exergy destruction rate compared to other system components. The effects of key parameters of the SOFC and ORC-VCR subsystems on the system performance are also analyzed. The results revealed that increasing current density increases SOFC net power and refrigeration capacity. Furthermore, by increasing the SOFC operating temperature, the refrigeration capacity increases. However, an optimum value for the cell operating temperature produces the maximum SOFC net power.

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## 1. Introduction

The reduction in fossil fuels, environmental issues, global warming, and the need for more efficient systems have resulted in consideration of new energy sources over the past few decades [1, 2]. Among many renewable energies, solid oxide fuel cells have several benefits like high efficiency, high operating temperature, low noise and pollution, and high power density [3-8]. Besides, due to the high exhaust temperature in this component, its waste gases have enough energy to be further recovered by other systems to produce power, refrigeration, hydrogen, fresh water, etc. [9-22]. Wang et al. [23] introduced a hybrid system in which the waste energy of a SOFC-GT was delivered to a Kalina cycle. They investigated the effect of different parameters like compressor pressure ratio and air flow rate on the system's performance. Yan et al. [24] integrated a SOFC, a gas turbine, and an ORC with LNG as a heat sink to generate more power. The net system electrical efficiency was reported at 67%. Zhao et al. [25] studied a CCHP combined with a SOFC to obtain more efficiency. They indicated that the electrical efficiency of the SOFC, the total power efficiency, and the overall efficiency of the SOFC-CCHP are 60%, 70%, and 90%, respectively. Chitsaz et al. [26] introduced four different hybrid systems based on a SOFC. Energy, exergy, and economic analysis were performed, and the results were compared for different configurations. They demonstrated that the cathode and anode gas recycling system produced better results. Chitgar et al. [27] employed a Kalina cycle, a SOFC, and a thermoelectric generator in a hybrid system. The power generated by the Kalina and thermoelectric

generator was transmitted to a reverse osmosis desalination system. The total cost rate and energy efficiency were reported as 36.8 \$/hr and 54%, respectively.

Emadi et al. [28] proposed a hybrid system based on a dual loop ORC and SOFC-GT. An LNG system was also used as the ORC's heat source, and some electricity was produced through the LNG turbine. The system performance was evaluated for different working fluids in the ORC. Adebayo et al. [29] proposed a mutigeneration system consisting of a cascaded closed loop ORC, a SOFC, a LiBr/water absorption refrigeration system, a biogas digester, and a PEM electrolyzer; the SOFC was the main mover. They investigated the thermodynamic performance of the system for different design parameters. Zeng et al. [30] presented a hybrid system based on a SOFC, a gas turbine, an ORC, and a double-effect absorption refrigeration system. They obtained 48.2%, 63.2%, and 62.67% for SOFC electrical efficiency and the system's overall electrical and exergy efficiency, respectively. Zhong et al. [31] proposed a hybrid system based on a SOFC, supercritical CO<sub>2</sub> system, and an ejector refrigeration system. The results showed that the SOFC has the highest cost and exergy destruction rate compared to the other subsystems. Dhahad et al. [32] proposed a novel CCP system based on a SOFC, an ejector, and an absorption refrigeration system. They stated that increasing the evaporation temperature, the ammonia concentration, and the SOFC inlet temperature can result in higher exergy productivity. Mei et al. [33] employed a thermoelectric generator and an absorption refrigeration system to use the waste energy of a SOFC system. They introduced

four different configurations for the system and compared their thermodynamic performances. Song et al. [34] employed a Rankin and Kalina cycle as the top and bottom systems to achieve the waste energy of a SOFC. The genetic algorithm was employed to optimize the thermodynamic parameters. The generated power of the SOFC, Kalina cycle, and Rankin cycle was 145 kW, 59.39 kW, and 170.1 kW, respectively.

As mentioned above, many studies have been done on integrating a SOFC with other thermodynamic systems, and the design of multipurpose systems has always been of great importance. The present research investigates a novel integrated system that integrates a SOFC system with two ORC-VCR subsystems. The proposed cogeneration system has the ability to produce power or combined power and refrigeration in a wide range of refrigeration temperatures. Thermodynamic modeling is conducted to obtain energy and exergy efficiencies of the system. Additionally, a parametric analysis is carried out to investigate the effect of important parameter variations on system performance.

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## 2. System description

Fig. 1 illustrates the CCP system considered in the present work. The SOFC unit produces power and the two ORC-VCR subsystems supply refrigeration employing the energy of waste gases from the SOFC. Air and fuel (methane) enter the air compressor (AC) and fuel compressor (FC), respectively, and reach the required pressure of the SOFC. The air enters the cathode of the

SOFC after preheating in the HEX3. The fuel also preheats in the HEX2 and then mixes with water, which is pumped and passed through the HEX1. The mixed stream enters the anode of the SOFC. Due to electrochemical reactions occurring in the SOFC unit, DC current is produced. Then, an inverter will convert it to AC current. After finishing the electrochemical reactions in the SOFC, the unreacted fuel and excess air reach the afterburner, where the high-temperature combustion gases and pressure preheat the water, the fuel, and the air, respectively. Since the flue gases retain a high temperature after passing through the HEX3, they can enter the vapor generator I of a combined ORC-VCR system with a regenerator to produce refrigeration. The organic fluid superheated in vapor generator I enters turbine I to generate power and mixes with the compressor I outlet after passing through the regenerator (HEX4) before flowing to the condenser. The saturated liquid exiting the condenser splits into two streams. One stream goes to the vapor generator I, and the other passes through expansion valve I and enters evaporator I. The saturated vapor outlet of the evaporator enters the compressor and is pressurized to the condenser pressure. The flue gases exiting vapor generator I then flows to vapor generator II to run the second ORC-VCR system in which the regenerator is removed due to operating temperature.

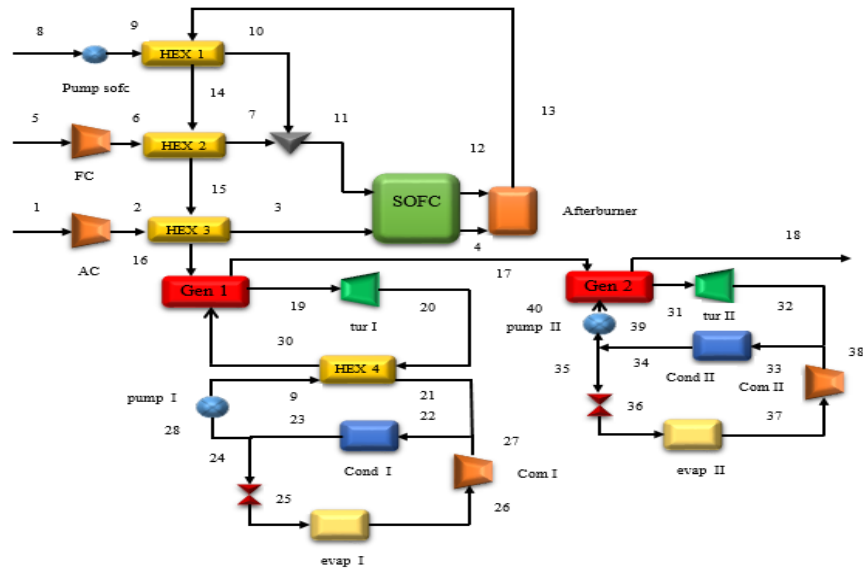


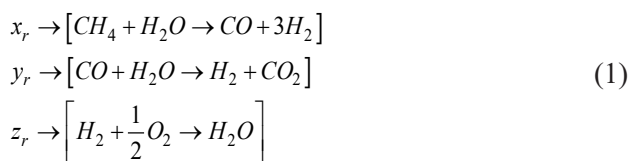
Fig. 1. The schematic of the SOFC integrated with two ORC-VCR systems.

### 3. Thermodynamic modeling

Some of the thermodynamic simulation assumptions are listed as follows [23, 26, 27, 29, 32] :

- The system reaches a steady condition.
- The air consists of 79% N<sub>2</sub> and 21% O<sub>2</sub>.
- Fuel and air entering the SOFC have equal temperature and pressure.
- The constant resistance and the pressure change throughout the SOFC are neglected.
- The unreacted gases are completely oxidized in the afterburner.
- The pressure losses in the pipelines and heat exchangers are neglected.

The reactions that occurred in the SOFC are as follows:



Where  $x_r$ ,  $y_r$ , and  $z_r$  denote the level of the reforming reaction, shifting reaction, and overall reaction, respectively. Equation (2) indicates the required equations for mass balance in the main components of the system:

$$\begin{aligned}
 \dot{n}_{CH_4,in} &= x_r \\
 \dot{n}_{H_2O,in} &= 2.5x_r \\
 \dot{n}_{H_2,out} &= 3x_r - y_r - z_r \\
 \dot{n}_{CO,out} &= x_r - y_r \\
 \dot{n}_{CO_2,out} &= y_r \\
 \dot{n}_{H_2O,out} &= 2.5x_r - y_r - z_r \\
 z_r &= U_f (3x_r + y_r)
 \end{aligned}
 \tag{2}$$

Where  $n$  is the molar flow rate and  $U_f$  depicts the fuel consumption factor. The following equation shows the SOFC stack work:

$$\dot{W}_{FC,stack} = N_{cell} \cdot I \cdot V_{cell}
 \tag{3}$$

Where  $V_{cell}$  represents the voltage of the fuel cell and can be derived as:

$$V_{cell} = V_N - V_{loss} \tag{4}$$

Where  $V_N$  is reversible voltage and  $V_{loss}$  depicts the voltage losses. The relations required to compute the voltage of the fuel cell are presented in Table 1.

**Table 1. Calculation of  $V_{cell}$ .**

Voltage	Relation
<b>Nernst voltage</b>	$E_{Nernst} = \frac{-\Delta G^0}{n_e F} + \frac{RT_{fc}}{n_e F} \ln \left( \frac{P_{H_2} (P_{O_2})^{0.5}}{P_{H_2O}^{sat}} \right)$
<b>Ohmic voltage</b>	$V_{loss} = V_{act} + V_{ohm} + V_{conc}$ $V_{ohm} = (\rho_a l_a + \rho_c l_c + \rho_e l_e + \rho_{int} l_{int}) i$ $\rho_a = \left( \frac{95 \times 10^6}{T_{cell}} \exp \left( \frac{-1150}{T_{cell}} \right) \right)^{-1}$ $\rho_c = \left( \frac{42 \times 10^6}{T_{cell}} \exp \left( \frac{-1200}{T_{cell}} \right) \right)^{-1}$ $\rho_e = \left( 3.34 \times 10^4 \exp \left( \frac{-10300}{T_{cell}} \right) \right)^{-1}$ $\rho_{int} = \left( \frac{9.3 \times 10^6}{T_{cell}} \exp \left( \frac{-1100}{T_{cell}} \right) \right)^{-1}$
<b>Activation voltage</b>	$V_{act} = V_{act,a} + V_{act,c}$ $V_{act,a} = \frac{RT_{cell}}{F} \left( \sinh^{-1} \left( \frac{i}{2i_{oa}} \right) \right)$ $V_{act,c} = \frac{RT_{cell}}{F} \left( \sinh^{-1} \left( \frac{i}{2i_{oc}} \right) \right)$
<b>Concentration voltage</b>	$V_{conc} = V_{conc,a} + V_{conc,c}$ $V_{conc,a} = \frac{-RT_{cell}}{2F} \left( \ln \left( 1 - \frac{i}{i_{as}} \right) - \ln \left( 1 - \frac{P_{H_2} i}{P_{H_2O} i_{as}} \right) \right)$ $V_{conc,c} = \frac{-RT_{cell}}{4F} \left( \ln \left( 1 - \frac{i}{i_{cs}} \right) \right)$ $i_{as} = \frac{4FP_{H_2} D_{aeff}}{RT_{cell} l_a}$ $i_{cs} = \frac{4FP_{O_2} D_{ceff}}{RT_{cell} l_c \left( 1 - \frac{P_{O_2}}{P_0} \right)}$

The current and current density of the SOFC stack can be written as:

$$I = i \cdot A_a$$

$$i = \frac{2 \cdot F \cdot z_r}{N_{cell} \cdot A_a} \tag{5}$$

Where  $F$ ,  $N_{fc}$ , and  $A_a$  are the Faraday, constant, and number of cells, respectively. The energetic analysis is based on the first law of thermodynamics and can determine the heat transfer and work rate occurring in each system component. Moreover, the exergy analysis, based on the second law of thermodynamics, is essential to identify losses, wastes, and irreversibilities arising in the system. In order to analyze the system's energy and exergy performance, the mass balance and the energy and exergy equations are applied to each system component.

$$\sum \dot{m}_i - \sum \dot{m}_e = 0 \tag{6}$$

$$\sum \dot{m}_i h_i - \sum \dot{m}_e h_e + \sum \dot{Q} - \sum \dot{W} = 0 \tag{7}$$

$$\dot{E}_d = \dot{E}_{in} - \dot{E}_{out} + \dot{E}_Q + \dot{E}_W \tag{8}$$

The exergy of each point of the system can be obtained as follows:

$$ex = ex_{ph} + ex_{ch} \tag{9}$$

Where  $ex_{ph}$  and  $ex_{ch}$  depicts physical and chemical exergy, respectively, which can be expressed using the following equations:

$$ex_{ph} = (h - h_0) - T_0 (s - s_0) \tag{10}$$

$$ex_{ch} = \sum x_n ex_{ch,n} + RT_0 \sum x_n \ln x_n \tag{11}$$

Where  $x_n$  is the mole fraction of species  $n$ , and  $ex_{ch,n}$  is the chemical exergy of species  $n$  in a dead state. The standard chemical exergies can be found in [35]. The equations for energy and exergy of each part of the system are presented in Table 2.

Table 2. Exergy and exergy equations for the system components.

Component	Energy equation	Exergy equation
HEX I	$\dot{Q}_{HEX1} = \dot{m}_{13} (h_{13} - h_{14})$	$\dot{E}x_9 - \dot{E}x_{10} + \dot{E}x_{13} - \dot{E}x_{14} = \dot{E}_{D,HEX1}$
HEX 2	$\dot{Q}_{HEX2} = \dot{m}_{13} (h_{14} - h_{15})$	$\dot{E}x_6 - \dot{E}x_4 + \dot{E}x_{14} - \dot{E}x_{15} = \dot{E}_{D,HEX2}$
HEX 3	$\dot{Q}_{HEX3} = \dot{m}_{13} (h_{15} - h_{16})$	$\dot{E}x_2 - \dot{E}x_3 + \dot{E}x_{15} - \dot{E}x_{16} = \dot{E}_{D,HEX3}$
AC	$\dot{W}_{AC} = \dot{m}_1 (h_2 - h_1)$ $\eta_{AC} = \frac{h_{2s} - h_1}{h_2 - h_1}$	$\dot{E}x_1 + \dot{W}_{AC} = \dot{E}x_2 + \dot{E}_{D,AC}$
FC	$\dot{W}_{FC} = \dot{m}_5 (h_6 - h_5)$ $\eta_{FC} = \frac{h_{6s} - h_5}{h_6 - h_5}$	$\dot{E}x_5 + \dot{W}_{FC} = \dot{E}x_6 + \dot{E}_{D,FC}$
Pump sofc	$\dot{W}_{pump,sofc} = \dot{m}_8 (P_9 - P_8) / \rho \eta_p$ $\dot{W}_{Pump,sofc} = \dot{m}_8 (h_9 - h_8)$	$\dot{E}x_8 = \dot{E}x_9 - \dot{W}_{Pump,sofc} + \dot{E}_{D,pump,sofc}$
Mixer	$\dot{m}_{11} h_{11} = \dot{m}_7 h_7 + \dot{m}_{10} h_{10}$	$\dot{E}x_7 + \dot{E}x_{10} = \dot{E}x_{11} + \dot{E}_{D,Mixer}$
SOFC	$\dot{Q}_{exp} = \dot{m}_7 (h_8 - h_7)$	$\dot{E}x_3 - \dot{E}x_4 + \dot{E}x_{11} - \dot{E}x_{12} = \dot{E}_{D,SOFC}$
Afterburner	$h_6 = h_7$	$\dot{E}x_4 + \dot{E}x_{12} = \dot{E}x_{13} + \dot{E}_{D,Afterburner}$
Generator I	$\dot{Q}_{genI} = \dot{m}_{16} (h_{16} - h_{17}) = \dot{m}_{30} (h_{19} - h_{30})$	$\dot{E}x_{16} - \dot{E}x_{17} + \dot{E}x_{30} - \dot{E}x_{19} = \dot{E}_{D,GeneratorI}$
Turbine I	$\dot{W}_{turI} = \dot{m}_{19} (h_{19} - h_{20})$	$\dot{E}x_{19} = \dot{E}x_{20} + \dot{W}_{turI} + \dot{E}_{D,turI}$
Evaporator I	$\dot{Q}_{evapI} = \dot{m}_{25} (h_{26} - h_{25})$	$\dot{E}x_{25} + \dot{Q}_{evapI} \left( 1 - \frac{T_0}{T_{evpI}} \right) = \dot{E}x_{26} + \dot{E}_{D,evpI}$
Condenser I	$\dot{Q}_{condI} = \dot{m}_{22} (h_{22} - h_{23})$	$\dot{E}x_{22} + \dot{Q}_{condI} \left( 1 - \frac{T_0}{T_{condI}} \right) = \dot{E}x_{23} + \dot{E}_{D,CondI}$
Expansion valve I	$h_{24} = h_{25}$	$\dot{E}x_{24} = \dot{E}x_{25} + \dot{E}_{D,ValveI}$
HEX 4	$h_{20} - h_{21} = h_{30} - h_9$	$\dot{E}x_{20} - \dot{E}x_{21} + \dot{E}x_9 - \dot{E}x_{30} = \dot{E}_{D,HEX4}$
Generator II	$\dot{Q}_{genII} = \dot{m}_{16} (h_{17} - h_{18}) = \dot{m}_{40} (h_{31} - h_{40})$	$\dot{E}x_{17} - \dot{E}x_{18} + \dot{E}x_{40} - \dot{E}x_{31} = \dot{E}_{D,GeneratorII}$
Turbine II	$\dot{W}_{turII} = \dot{m}_{31} (h_{31} - h_{32})$	$\dot{E}x_{31} = \dot{E}x_{32} + \dot{W}_{turII} + \dot{E}_{D,turII}$
Evaporator II	$\dot{Q}_{evapII} = \dot{m}_{36} (h_{37} - h_{36})$	$\dot{E}x_{36} + \dot{Q}_{evapII} \left( 1 - \frac{T_0}{T_{evpII}} \right) = \dot{E}x_{37} + \dot{E}_{D,evpII}$
Condenser II	$\dot{Q}_{condII} = \dot{m}_{33} (h_{33} - h_{34})$	$\dot{E}x_{33} + \dot{Q}_{condII} \left( 1 - \frac{T_0}{T_{condII}} \right) = \dot{E}x_{34} + \dot{E}_{D,CondII}$
Expansion valve II	$h_{35} = h_{36}$	$\dot{E}x_{35} = \dot{E}x_{36} + \dot{E}_{D,ValveII}$

The efficiency of the ORC-EVCR and the total efficiency of the system can be calculated through the following equations:

$$COP = \frac{\dot{Q}_{evp}}{\dot{Q}_{gen} + \dot{W}_{pump}} \tag{12}$$

$$\eta_{SOFC} = \frac{\dot{W}_{SOFC} - \dot{W}_{AC} - \dot{W}_{FC} - \dot{W}_{pump,sofc}}{(\dot{m}_{H_2,cons}) \cdot LHV_{CH_4}} \tag{13}$$

$$\eta_{Overall} = \frac{\dot{W}_{SOFC} - \dot{W}_{AC} - \dot{W}_{FC} - \dot{W}_{pump,sofc} + \dot{Q}_{evpl} + \dot{Q}_{evpll} - \dot{W}_{pumpI} - \dot{W}_{pumpII}}{(\dot{m}_{H_2,cons}) \cdot LHV_{CH_4}} \tag{14}$$

Moreover, the exergy efficiency of the ORC-EVCR, PEM fuel cell, and total system can be calculated as follows:

$$\eta_{x,SOFC} = \frac{\dot{W}_{SOFC} - \dot{W}_{AC} - \dot{W}_{FC} - \dot{W}_{pump,sofc}}{(\dot{E}x_3 + \dot{E}x_{11}) - (\dot{E}x_4 + \dot{E}x_{12})} \tag{15}$$

$$\eta_{x,ORC-EVCRI} = \frac{\dot{Q}_{evpl} \left(1 - \frac{T_0}{T_{evpl}}\right)}{(\dot{E}x_{16} + \dot{E}x_{17}) - (\dot{E}x_{30} + \dot{E}x_{19}) + \dot{W}_{pumpI}} \tag{16}$$

$$\eta_{x,ORC-EVCRII} = \frac{\dot{Q}_{evpll} \left(1 - \frac{T_0}{T_{evpll}}\right)}{(\dot{E}x_{17} + \dot{E}x_{18}) - (\dot{E}x_{40} + \dot{E}x_{31}) + \dot{W}_{pumpII}} \tag{17}$$

$$\eta_{x,overall} = \frac{\dot{W}_{SOFC} - \dot{W}_{AC} - \dot{W}_{FC} - \dot{W}_{pump,sofc} + \dot{Q}_{evpl} \left(1 - \frac{T_0}{T_{evpl}}\right) + \dot{Q}_{evpll} \left(1 - \frac{T_0}{T_{evpll}}\right) - \dot{W}_{pumpI} - \dot{W}_{pumpII}}{(\dot{E}x_3 + \dot{E}x_{11}) - (\dot{E}x_4 + \dot{E}x_{12})} \tag{18}$$

### 4. Results and discussion

This section presents and discusses the thermodynamic modeling results and the effect of variations in important parameters on system performance. The EES program was employed to perform all thermodynamic computations. In order to validate the mathematical

model of the proposed system, the SOFC voltage is compared with data presented by Ref [29]. According to Fig. 2, there is an acceptable agreement between the results of the current study and those reported by [29]. Moreover, the ORC-VCR simulation was verified by comparing the main thermodynamic parameters with the results from [36] for the R245fa refrigerant. As can be seen in Table 3, the maximum deviation is 0.35%, which indicates good consistency between the results. The required input parameters for simulation are listed in Table 4. Considering the temperature range, cyclohexane and propane were selected as the working fluid in the ORC-VCR 1 and ORC-VCR2 subsystems, respectively. Table 5 shows that the SOFC system can generate 382.4 kW power. In addition, 159.9 kW and 16.38 kW of refrigeration load can be produced by integrating two ORC-VCRI and ORC-VCRII subsystems, respectively. Moreover, the proposed system's overall energy and exergy efficiencies are 68.96% and 81.89%, respectively, 45.82% and 6.14% higher than the stand-alone SOFC system. Fig. 3 represents the distribution of exergy destruction rate for each system component. It can be observed that the largest amount of exergy destruction occurs in the HEX3, which is about 20.41% of the total exergy destruction rate. Furthermore, the afterburner, SOFC stack, and evaporator I also have considerable destroyed exergy, which should be considered in the design and application of the system.

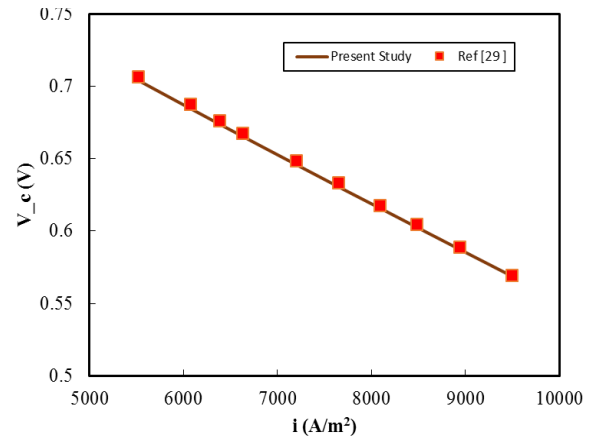


Fig. 2. SOFC voltage verification by [29].



**Table 3. Comparison of ORC-VCR cycle parameters with Ref [36]**

Parameter	Present study	Ref [36]	Deviation (%)
$\dot{W}_{\text{turbine}}$ (kW)	31.35	31.39	0.12
$\dot{Q}_{\text{evp}}$ (kW)	158.57	158.7	0.08
$\text{COP}_s$	0.5815	0.582	0.08
$\mathfrak{z}_x$ (%)	30.57	30.68	0.36

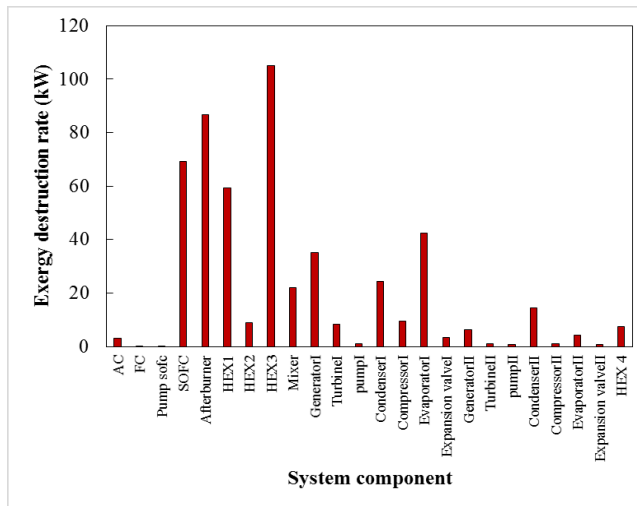
**Table 4. The input parameters for the simulation [26, 29, 32].**

Parameter	Value
Farady Constant, F	96485 (C/mol)
Number of electrons, $n_e$	2
Number of cells, $N_{\text{cell}}$	13000
Difference temperature between inlet and outlet of SOFC	100 (°C)
Active surface area, $A_a$	0.01 (m <sup>2</sup> )
Current density	5500 (A/ m <sup>2</sup> )
Anode exchange current density, $i_{\text{oa}}$	6500 (A/ m <sup>2</sup> )
Cathode exchange current density, $i_{\text{oc}}$	2500 (A/ m <sup>2</sup> )
$\eta_{\text{inv}}$	95 %
Effective anode gaseous diffusivity, $D_{\text{aeff}}$	$0.2 \times 10^{-4}$ (m <sup>2</sup> /s)
Effective cathode gaseous diffusivity, $D_{\text{ceff}}$	$0.05 \times 10^{-4}$ (m <sup>2</sup> /s)
Fuel utilization factor, $U_f$	0.8
Anode thickness, $l_a$	0.05 (cm)
Cathode thickness, $l_c$	0.005 (cm)
Electrolyte thickness, $l_e$	0.001 (cm)
Interconnect thickness, $l_{\text{int}}$	0.3 (cm)
Steam to carbon ratio, $r_{\text{sc}}$	2
Afterburner efficiency, $\eta_{\text{AB}}$	99 %
$\eta_{\text{AC}}$	85 %
$\eta_{\text{FC}}$	85 %
$\eta_p$	85 %
Inlet pressure of turbine I	622 kPa
Inlet pressure of turbine II	2667 kPa
Degree of superheat	10 (°C)
Pinch point temperature in generators	10 (°C)



**Table 5. Result of energy and exergy analysis for the proposed system.**

Parameter	Value
SOFC voltage (V)	0.7049
SOFC net electrical power (kW)	382.4
SOFC energy efficiency (%)	47.29
SOFC exergy efficiency (%)	77.15
SOFC exergy destruction rate (kW)	354.87
ORC-VCRI COP	0.79
$\dot{Q}_{evpI}$ (kW)	159.9
ORC-VCRI exergy efficiency	24.09
ORC-VCRI exergy destruction rate (kW)	131.5
ORC-VCRII COP	0.27
$\dot{Q}_{evpII}$ (kW)	16.38
ORC-VCRII exergy efficiency (%)	15.64
ORC-VCRII exergy destruction rate (kW)	29.04
Overall energy efficiency (%)	68.96
Overall exergy efficiency (%)	81.89
Overall exergy destruction rate (kW)	515.41



**Fig. 3. Exergy destruction rates of the system components.**

### 5. Parametric Study

Fig. 4 shows the variations of SOFC net power generation and the refrigeration capacity of the system while the other operating parameters are kept constant. As observed, the net power generation of the SOFC and

refrigeration capacity increases with increasing the current density. Increasing the fuel cell current density increases the voltage losses, leading to a reduction in the fuel cell voltage. However, the effect of increasing the current density is more prominent than decreasing the fuel cell voltage. Therefore, the net power of the

SOFC increases with increasing the current density. Furthermore, increasing the current density increases the molar flow rate to the SOFC, which increases heat energy delivered to the two ORC-VCR subsystems, raising the refrigeration capacity. However, as can be observed from Fig. 4b, the energy and exergy efficien-

cy of the system decrease with increasing the current density. This is because increasing the rate of inlet energy and exergy is greater than outlet energy and exergy from the fuel cell. Hence, the efficiency of the SOFC and the total system efficiency decrease.

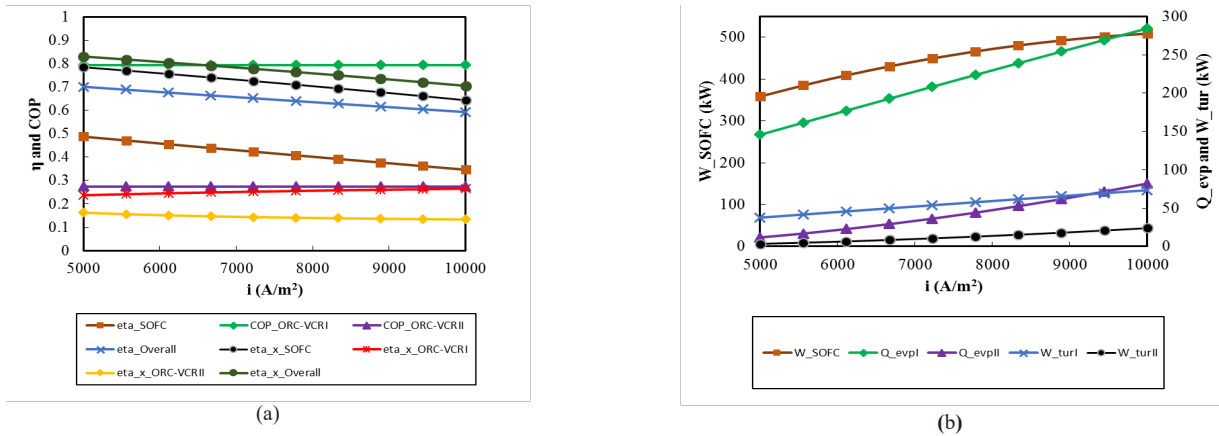


Fig. 4. Effect of current density variation on a) system performance and b) power and refrigeration capacity.

The variations in the system performance with fuel cell inlet temperature are displayed in Fig. 5. As can be observed from Fig. 5a, increasing the fuel cell inlet temperature first increases then decreases the fuel cell output power. This is because increasing the fuel cell inlet temperature causes a decrease in the Ohm voltage and increases the activation and concentration voltages. Hence, there is an optimum value for the fuel cell voltage and fuel cell power. Referring to Fig. 5b,  $Q_{evpI}$  increases and  $Q_{evpII}$  decreases with increas-

ing the fuel cell inlet temperature. At higher fuel cell inlet temperatures, the temperature of the fuel cell's exhaust gases increase, which leads to an increase in the inlet temperature of turbine I and, consequently, the refrigeration capacity of cycle I increases. On the other hand, increasing generator I's inlet temperature decreases the temperature of its outlet stream, which causes a decrease in the power of turbine II, decreasing the refrigeration capacity of cycle II.

Fig. 6 depicts the effect of the utilization factor on system performance. Referring to Fig. 6a, increasing

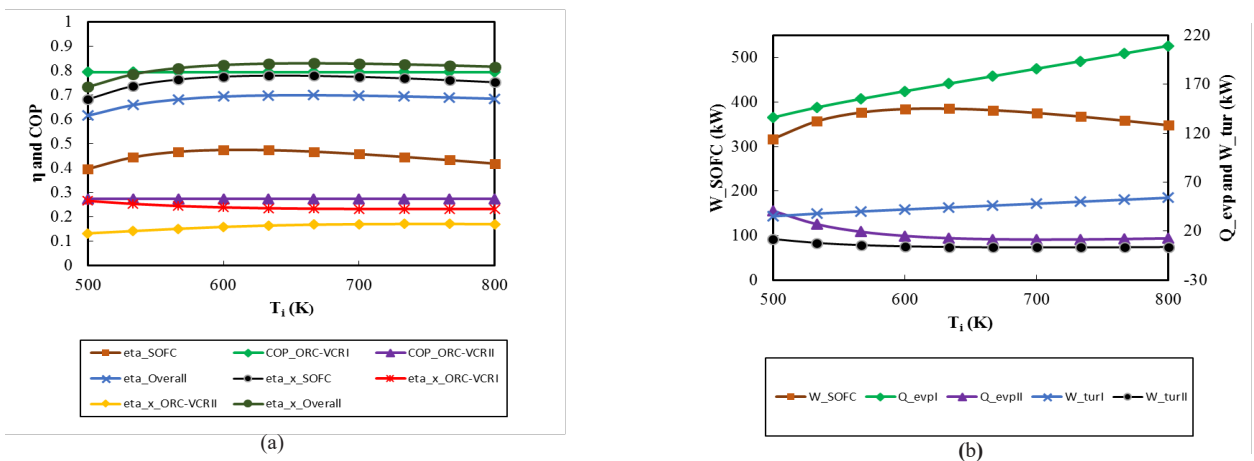


Fig. 5. Effect of fuel cell temperature variation on a) system performance and b) power and refrigeration capacity.

the fuel utilization factor decreases the SOFC net power and the refrigeration capacity. The reason is that in higher fuel utilization factors, the molar input rate of the fuel to the SOFC decreases, and the molar input rate of the air to the SOFC increases. Moreover, due to the participating hydrogen in the reactions, the partial pressure of the hydrogen and oxygen decreases, leading to a decrease in the SOFC voltage. Therefore, the output power of the SOFC decreases by increasing the fuel utilization factor. On the other hand, increasing the fuel utilization factor decreases the input energy to the ORC-VCR subcycles, which lowers the refrigeration capacity. However, the energy efficiency of

the total system first increases and then declines as the utilization factor increases. This is because the reduction in the input fuel flow rate dominates the decreasing SOFC power. However, at higher utilization factors, the reduction of the input fuel flow rate cannot compensate for the reduced SOFC power, and the energy efficiency of the SOFC and hybrid system decline. Moreover, increasing the utilization factor decreases the exergy difference between the inlet and outlet streams of the SOFC. However, the reduction in power generation and refrigeration capacity is more prominent. Therefore, the exergy efficiency of the SOFC and the total system decrease as the utilization factor increases.

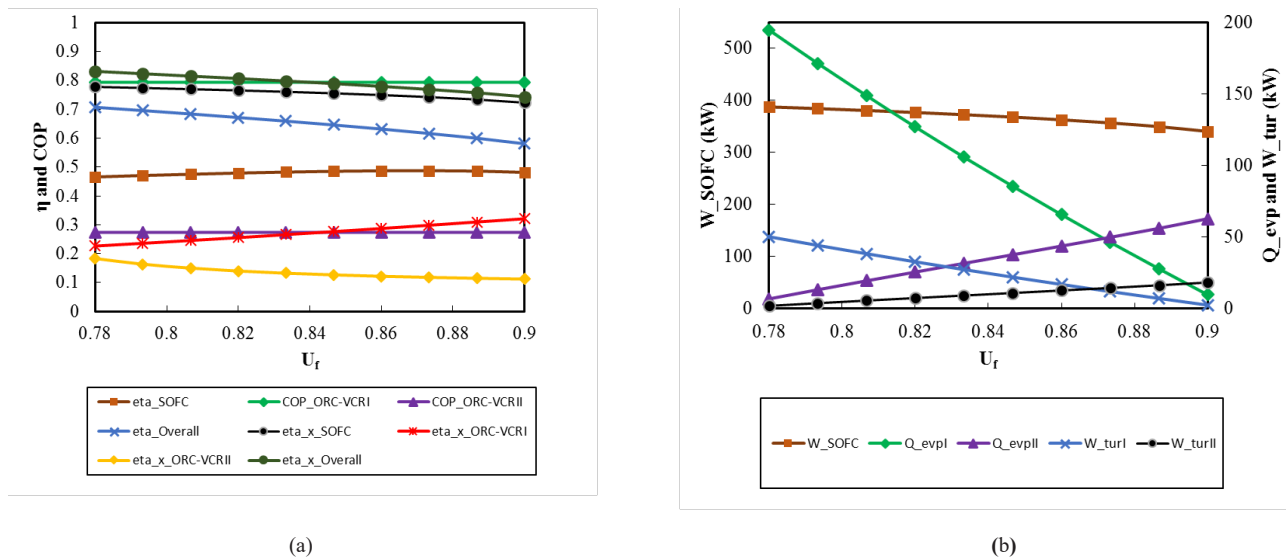


Fig. 6. Effect of fuel utilization factor variation on a) system performance and b) power and refrigeration capacity.

The effect of the maximum pressure of the ORC-VCR I subcycle on system performance is displayed in Fig. 7. According to Fig. 6a, an increase in the inlet pressure of turbine I decreases the  $Q_{evpl}$  and increases the  $Q_{evplII}$ . Increasing the maximum pressure in ORC-VCR I at constant pinch temperature in generator I increases the output temperature of generator I, decreasing en-

ergy delivery to the ORC-VCR I and the refrigeration capacity. However, increasing the output temperature of the gases exiting generator I transfers more energy to the ORC-VCR II, and  $Q_{evplII}$  increases. Referring to Fig. 4b, there is an optimum value for the maximum pressure of the ORC-VCR I cycle at which the energy and exergy efficiencies of the system are maximum.

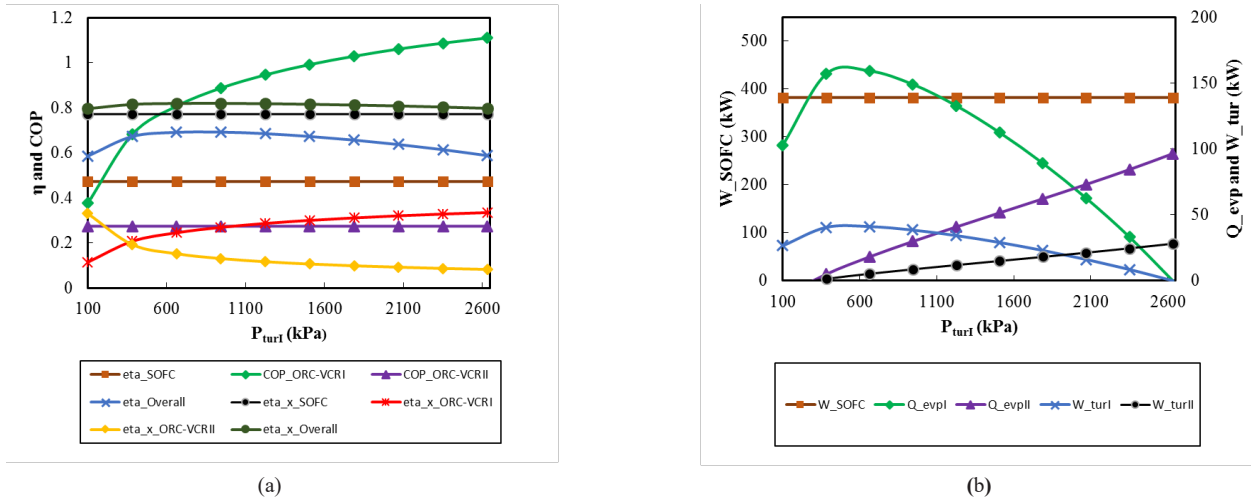


Fig. 7. Effect of turbine I pressure variation on a) system performance and b) power and refrigeration capacity.

Fig. 8 depicts the effect of turbine II inlet pressure on system performance. As can be observed from Fig. 8a, the refrigeration capacity of ORC-VCRII increases as the maximum pressure increases. Whereas the SOFC

and the ORC-VCRI parameters remain constant, the energy and exergy efficiencies of the system are enhanced at higher ORC-VCRI II subsystem maximum pressures.

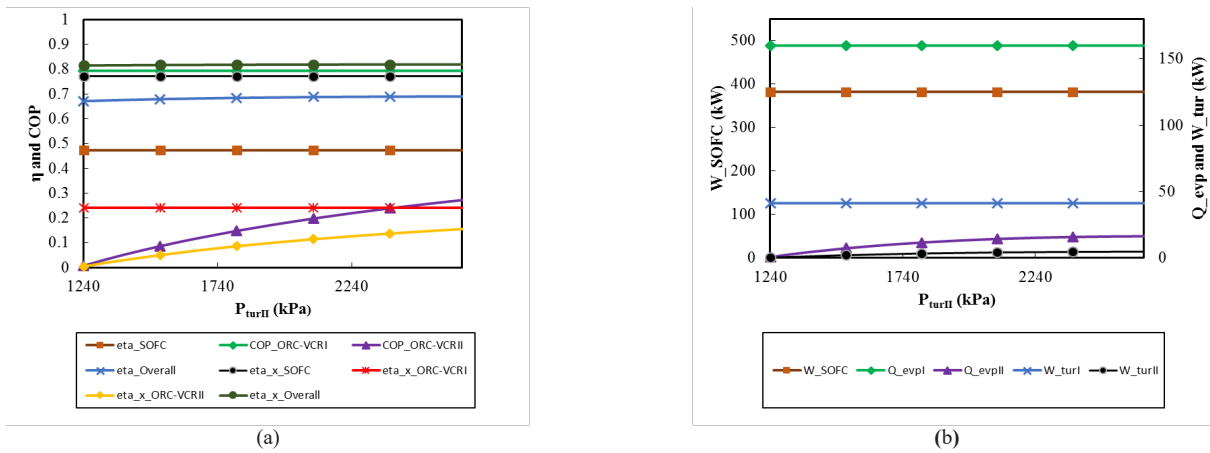


Fig. 8. Effect of turbine II pressure variation on a) system performance and b) power and refrigeration capacity.

The impacts of evaporating temperature on system performance are displayed in Fig. 9. As can be seen, the energy and exergy efficiencies of the refrigeration capacity of both subsystems improve as the evaporator temperature rises. As the input energy to both ORV-VCR subsystems is constant, the variation of evaporator temperature has no influence on ORC sections. However, increasing the evaporator temperature increases the evaporator pressure, which leads to a reduction in required compressor power. Therefore, the mass flow rate

of the refrigeration section increases. On the other hand, raising the evaporator pressure causes an increase in the enthalpy difference between the inlet and outlet streams of the evaporator. Increasing the mass flow rate and enthalpy difference along the evaporator improves the refrigeration capacity. As input parameters of the system are constant, energy and exergy efficiencies are enhanced as the evaporator temperature increases.

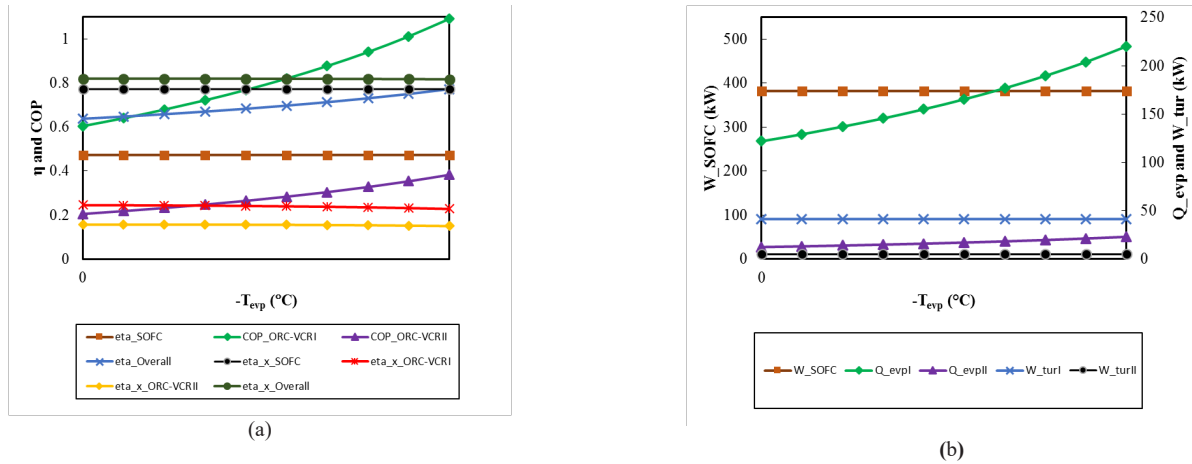


Fig. 9. Effect of evaporator temperature variation on a) system performance and b) power and refrigeration capacity.

## Conclusion

This work presents a CCP system consisting of a solid oxide fuel cell and two subsystems based on an organic Rankin cycle and vapor compression system. The SOFC produces electrical power, and the ORC-VCR subsystems use the waste heat of the solid oxide cell as a heat source to provide refrigeration. The energy and exergy efficiency of the proposed system was then compared to a stand-alone SOFC system. Afterward, a parametric study was carried out to investigate the effect of key thermodynamic parameters of the SOFC and ORC-VCR on system performance. The main conclusions of the present study can be summarized as follows:

- The system's overall energy and exergy efficiency is 45.82% and 6.14% higher than a stand-alone SOFC system.
- The refrigeration capacity and the energy and exergy efficiencies improve with rising the evaporator temperature.
- The net power generation of the SOFC and refrigeration capacity increases as the current density increases.
- There is an optimum cell operating temperature value to produce the maximum SOFC net

power. This temperature for the mentioned input parameters is about 633 K.

- The SOFC net power and the refrigeration capacity decrease as the fuel utilization factor increases. Furthermore, the exergy efficiency of the SOFC and the total system decrease as the utilization factor increases.
- Overall, the system performance is enhanced at higher ORC-VCR II subsystem maximum pressures. However, there is an optimum maximum pressure value for the ORC-VCRI cycle at which the efficiencies of the system are maximum.

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